PANEL FLUTTER CONTROL AT HIGH SUPERSONIC SPEED USING PIEZOELECTRIC MATERIAL

التحكم في رفرفة الألواح التي تعمل على سرعات تفوق سرعة الصوت باستخدام مواد البيزوالكتريك

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الخلاصة

تتعرض الألواح الخارجية المكونة للكساء الخارجي للمركبات التي تطير بسرعات أعلى من سرعة الصوت في الغلاف الخارجي لما يسمى بالإهتزازات المثارة ذاتيا من النوع ذو التربدات المحدودة. إن تطور الطرق المستخدمة في التحكم في هذه الظاهرة مطلوب وهو الهدف من هذه الدراسة.

وفى هذه الدراسة تم استخدام المعادلات اللاخطية للالواح بموائمة كل من نظرية الإنحناءات الكبيرة فى الألواح لفان كارمن والنظرية الإيروديناميكية الخطية السيال الهواء المنتظم على سطح الألواح لتناسب الحالة تحت الدراسة وهى عبارة عن لوح من الديور الومنيوم مثبت علية من كلا السطحين العلوى والسفلى مادة البيزو اليكتريك تتبيتا جيدا.

وعند تطبيق قدر مناسب من القولت على مادة البيز و اليكتريك فانه ينتج نوع من التمدد العرضى لمادة اللوح وبالتالى حدوث ما يسمى بقوى الشد و المؤثرة في مستوى اللوح. وهذه القوى تؤثر تاثيرا إيجابيا بترحيل نقطة تعرض اللوح لظاهرة الرفرفة الى قيمة أعلى من القيمة التي يعمل عندها اللوح بدون المعالجة التي أجريت عليه.

وفى هذه الدراسة تم إيضاح قيم فولت التحكم وكذلك خواص وتأثير مواد البيزو الكتريك على الالواح من خلال مقارنة النتائج الخاصة بظاهرة الرفرفة لللالواح بعد المعالجة وقبلها. وقد أثبتت النتائج في هذه الدراسة بنجاح النموذج المقترح بالتحكم في إيقاف ظاهرة الرفرفة لللالواح في ظروف عملها.

Abstract

Exterior panels forming the skin of flight vehicles traveling through the atmosphere at high supersonic speed are often susceptible to the occurrence of limit-cycle type self-excited vibrations called flutter. The development of methods for panel flutter control is desirable and it is the objective of this work by using piezoelectric materials.

The nonlinear equations of motion for panel flutter using Von-Karman's large deflection plate theory and the quasi-steady aerodynamic theory are modified to consider the composite plate with the piezoelectric layer. The composite plate consists of two piezoelectric layers bonded perfectly to the upper and lower surface of the original panel layer.

When a voltage is applied to the piezoelectric layers, an induced strain in the plate material take place and consequently tensile in-plane load is obtained. These tensile loads shift the onset of flutter point to about twice the value of the critical dynamic pressure for the plate alone.

The values of control voltage and the effect of piezoelectric material properties are investigated. The method gives good results and succeeds in suppressing the panel flutter at its operating condition.

KEY WORDS

Panel Flutter, Aerodynamic Loading, Aerodynamic Damping, Structural Damping, Cavity Effect, Thermal Effect, Smart Structure, Piezoelectric Material.

I. Introduction:

Panel flutter results from the interaction between the panel and the flow pressure forces brought about by the panel motion. This causes a loss of the stability of the panel in its un-deformed shape, so that any disturbance applied to it leads to oscillations of growing amplitude. Thus, it is a self excited oscillation resulting from the dynamic instability of the aerodynamic, inertia. and elastic forces of the system. This growth is limited, however, by the membrane tension stresses induced in the panel by the flutter motion itself. The result of this self-limiting action is a sustained oscillation of constant amplitude, called limit-cycle motion.

Due to the complexity of panel flutter, most theoretical studies make use of simplified assumptions, see Ref [13]. However these assumptions usually so restrictive that the theoretical model does not accurately represent realistic conditions. In fact it is found that the application of the exact aerodynamic theory does not remove the discrepancies that presently exist between theory and experiment for flutter of stressed panels. The inclusion of structural damping is found to have a large effect in some instances and can tend to eliminate some of the differences. Von Karman's deflection plate theory and quasisteady aerodynamic theory have been employed. Galerkin's technique has been used in the space variables and differential the ordinary system obtained is solved by method of describing functions/harmonic balance method or direct numerical integration. The results obtained show that, as a first approximation, the amplitude of the limit cycle depends only upon the fundamental parameter dimensional aerodynamic loading), the and the damping aspect ratio. (including structural parameter damping effect). The results are in

excellent agreement with those obtained numerically in Ref. [5].

Agreement between theory and experiment improves at the higher Mach numbers. The disagreements between theory and experiment are mainly due to four factors:

1-The use of linear aerodynamic theory. where most of the theoretical investigations have utilized twodimension static aerodynamic theory (both with and without damping). despite the fact that two dimensional theory is considered applicable only for a limited range of panel length-to-width ratio and Mach number.

2-Neglecting boundary layer and aerodynamic heating effects.

3-The imprecise idealization of the complicated panel support conditions and cavity.

4-Neglecting nonlinear mid-plane stresses and buckling.

Considering all of the above factors in formulating the mathematical model. the results of the theory and the experiment will be in excellent agreement. Flutter oscillations rarely cause immediate failure of the panel. but they may produce fatigue failure after a sufficient period of time. The need to prevent this occurrence, either by suppressing flutter entirely or by limiting the severity of the panel motion. often becomes the critical design criterion that determines the required thickness (or more generally stiffness) of the panel, see Ref [16]. parameters govern resonance fatigue behavior including the detail design, the skin thickness stiffener and materials. the configurations and the damping of the structure. The new technology for flutter prevention is to use piezoelectric actuators to produce an induced strain and, consequently, in-plane tensile forces to stabilize the plate during flutter. The plate with the piezoelectric actuators and sensors are called controlled structures (or smart structures), where both sensors and actuators are connected through a feedback loop, see Ref. [19] and [25]. There are two types of controlled structures called vibration control and shape control. Actually in vibration control, the objective is to change the dynamic properties of the structure, such as damping. To do this, relatively small forces can be exerted on many flexible modes by relatively small The number of actuators. common form of vibration control entails the addition of active damping by the feedback of measured or inferred rate to actuators, see Ref [20]. The purpose of such active damping is to reduce the response of the structure. Another concept, closely related to active damping is active stabilization, in which initially unstable modes are stabilized by closed loop control see Ref. [23].

II. Problem Formulation

The plate under consideration with cavity is shown in Fig. 1 with dimension and properties shown in Table. 3. The axes are taken to be such that the x-, yaxes are in the plane of the plate passing through its reference plane (z=0), while the z- axis is positive upwards. Under the assumptions that plate thickness is small in comparison with smallest lateral dimension, which is the case in most practical applications, the Kirchhoff's hypothesis may be assumed to be valid. With this assumption the in-plane displacements "u", "v" and the transverse deflection "w" at an arbitrary point of the plate in the x, y, and z directions will be as given in Ref. [13] and [27]. The plate aero-elastic equations in a nondimensional form are finally will be:

The U-equation is given as:

$$\overline{u}_{,\xi\xi}+d_1f^2\overline{u}_{,\eta\eta}+d_2f\overline{v}_{,\xi\eta}+\frac{h}{a}\{\overline{w}_{,\xi}\overline{w}_{,\xi\xi}+d_1f^2\overline{w}_{,\eta\eta}+d_2f^2\overline{w}_{,\eta}\overline{w}_{,\xi\eta}\}=0$$
(1-a)

The V-equation is given as:

$$d_{1}\overline{v}_{,\xi\xi}+f^{2}\overline{v}_{,\eta\eta}+d_{2}f\overline{u}_{,\xi\eta}+\frac{h}{b}\{f^{2}\overline{w}_{,\eta}\overline{w}_{,\eta\eta}+d_{2}f\overline{u}_{,\xi\eta}+\frac{h}{b}\{f^{2}\overline{w}_{,\eta}\overline{w}_{,\eta\eta}+d_{2}f\overline{u}_{,\xi\eta}\}=0$$

$$(1-b)$$

The W-equation is given as: $\frac{1}{\overline{\mathbb{T}^4}} \{ \overline{W}_{,\xi\xi\xi\xi} + 2f^2 \overline{W}_{,\xi\xi\eta\eta} + f^4 \overline{W}_{,\eta\eta\eta\eta} \} \pm \{$ $\overline{n}_{n}^{(AL)} + \overline{n}_{n}^{(AT)} \pm \{ \overline{n}_{\epsilon}^{(AL)} + \overline{n}_{\epsilon}^{(AT)} \} +$ $\lambda_{a}\overline{W}_{,\xi}+\lambda_{d}\overline{W}_{,\tau}+\lambda_{d}\int_{0}^{1}\sqrt{w}d\eta d\xi+\overline{W}_{,\tau}-\frac{1}{\pi}\{$ $12\frac{a}{h}[\overline{u}_{\xi}\overline{w}_{\xi\xi}+v^2\overline{u}_{\xi}\overline{w}_{\eta\eta}+(1-v)]f^2\overline{u}_{\eta\eta}$ $\overline{W}_{,\xi\eta}+f^3\overline{V}_{,\eta}\overline{W}_{,\eta\eta}+\nu f\overline{V}_{,\eta}\overline{W}_{,\xi\xi}+(1-\nu)f\overline{V}_{,\xi}$ $\overline{W}_{,\xi\eta}$]+6 $[\overline{W}^{2}_{,\xi}\overline{W}_{,\xi\xi}$ + $f^{4}\overline{W}^{2}_{,n}\overline{W}_{,nn}$ + $f^{2}\overline{W}^{2}_{,n}$

$$\overline{\mathbf{w}}_{,\xi\xi} + \mathbf{f}^2 \overline{\mathbf{w}}^2_{,\xi} \overline{\mathbf{w}}_{,\eta\eta} + \mathbf{f}^2 \overline{\mathbf{w}}_{,\xi} \overline{\mathbf{w}}_{,\eta} \overline{\mathbf{w}}_{,\xi\eta}] \} = 0$$
 (1-c)

Where, $d_1=(1-\nu)/2$ and $d_2=(1+\nu)/2$

The form of these equations is general see Ref [1] and Ref. [9]. Galerkin's method is then used to reduce the obtained equations of motion to a set of nonlinear ordinary differential equations having the non-dimensional variable as an independent variable. The displacement u, v, and the deflection ware expanded in the form of a generalized double series of modes. These modes satisfy the appropriate geometric boundary conditions of the plate, thus:

$$\bar{u}^{o}(\xi, \eta, \tau) = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \bar{U}_{mn}(\tau) X^{(u)}_{m}(\xi) Y^{(u)}_{n}(\eta)$$
 (2-a)

$$\bar{V}^{o}(\xi, \eta, \tau) = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \bar{V}_{mn}(\tau) X^{(v)}_{m}(\xi) Y^{(v)}_{n}(\eta) \qquad (2-b)$$

$$\overline{W}^{o}(\xi, \eta, \tau) = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \overline{W}_{mn}(\tau) X^{(w)}_{m}(\xi) Y^{(w)}_{n}(\eta)$$
 (2-c)

where $X(\xi)$ and $Y(\eta)$ are the modal functions that satisfy the boundary conditions imposed on u, v, or w in the ξ and n direction respectively.

$$\begin{array}{c} \overset{mn}{C1} \overset{mn}{W} + \lambda_{d} \overset{mn}{C1} \overset{mn}{W} + \lambda_{a} \overset{mn}{C2} \overset{mn}{W} + \lambda_{c} \overset{mn}{C3} \overset{mn}{W} + \\ \overset{mn}{C4} \overset{mn}{W} + \{ n_{\xi}^{(AL)} + n_{\xi}^{(AT)} \} \overset{mn}{C5} \overset{mn}{W} + \{ n_{\eta}^{(AL)} + \\ n_{\eta}^{(AT)} \} \overset{mn}{C6} \overset{mn}{W} + \overset{mn}{C7} \overset{mn}{U} \overset{mn}{W} + \\ \overset{mn}{C7} \overset{mn}{V} \overset{mn}{W} + \overset{mn}{C7} \overset{mn}{U} \overset{mn}{W} + \\ \overset{mn}{C7} \overset{mn}{V} \overset{mn}{W} + \overset{mn}{C7} \overset{mn}{V} \overset{mn}{W} = 0 \\ \overset{mn}{C1} \overset{mn}{V} \overset{mn}{W} \overset{mn}{V} \overset{mn}{V} \overset{mn}{V} \overset{mn}{V} \overset{mn}{V} = 0 \end{array}$$

The vectors $U_{mn}(\tau)$ and V_{mn} (τ) are computed algebraically and substituted in the modal equation in its tensorial form to yield the Duffing-type equation in the following form:

$$\begin{array}{ll} mn & mn & mn \\ C1 W + \lambda_d C2W + C3W \pm \{n_\xi^{(AL)} + n_\xi^{(AT)}\} \\ ij & mn, \tau ij & mn \end{array}$$

$$\overset{mn}{\underset{ij}{C4W}} \pm \{n_{\eta}^{(AL)} \!\!+\! n_{\eta}^{(AT)} \!\} \overset{mn}{\underset{ij}{C5}} \overset{mn}{\underset{mn}{W}} + \lambda_{a} \overset{mn}{\underset{ij}{C6}} \overset{mn}{\underset{mn}{W}}$$

$$+\lambda_{c} \overset{mn}{\underset{ij}{C7}} \overset{mn|prs}{\underset{mn}{W}} \overset{-}{\underset{ij}{W}} \overset{m}{\underset{mn}{W}} \overset{-}{\underset{pr}{W}} = 0 \tag{4}$$

nonlinear This tensorial ordinary differential equation represents a set of nonlinear ordinary differential equation which can not be solved exactly.

To complete the solution, the boundary conditions for the plate must specified. For the purpose comparison with the result obtained by the experimental report by Ref. [10], the boundary conditions are specified to be clamped all around with no in-plane movements, so that the out of plane boundary condition is fully-clamped and the in-plane boundary condition is edge-fixed, and these conditions are written as:

$$w=w_{\xi}=u^{0}=v^{0}=0$$
 at both x=0 & x=1 (5-a)

$$w=w_{,\eta}=u^0=v^0=0$$
 at both y=0 & y=1 (5-b)
And the modal functions are then given

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by:
$$X^{(u)}_{m}(\xi)=X^{(v)}_{m}(\xi)=\sin(m\pi\xi)$$
 (6-a)

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$$X^{(u)}_{m}(\xi) = X^{(v)}_{m}(\xi) = \sin(m\pi\xi)$$
 (6-a)
And $Y^{(u)}_{n}(\eta) = Y^{(v)}_{n}(\eta) = \sin(n\pi\eta)$ (6-b)

$$X^{(w)}_{m}(\xi) = \cosh \alpha_{m} \xi - \cos \alpha_{m} \xi - \gamma_{m} (\sinh \alpha_{m} \xi - \sin \alpha_{m} \xi)$$
 (6-c)

$$-y_m(\sinh\alpha_m\xi-\sin\alpha_m\xi) \qquad (6-c)$$
and:
$$Y^{(w)}_n(\eta)=\cosh\alpha_n\eta-\cos\alpha_n\eta$$

$$-y_n(\sinh\alpha_n\eta-\sin\alpha_n\eta)$$
 (6-d) where α_m and y_m are the coefficients for

the mth flexural mode and can be calculated from the following equation:

$$coshα_m cos α_m = 1$$
 (7-a)

$$cosh\alpha_m$$
- $cos\alpha_m\xi$ - γ_m ($sinh\alpha_m$

$$-\sin\dot{\alpha}_{\rm m})=0 \tag{7-b}$$

The values of these coefficients are given in Table 1, see also Ref. [13] and [27]. Once the displacement modal functions аге specified prescribed boundary conditions, coefficients of integration represented by the matrices A1 to A3, B1 to B3, C1 to C9, and T can be calculated numerically, see Ref [13] and [27]. The number of the terms in the assumed displacement series solution given by (2-a), (2-b), and (2-c) are arbitrary.

Since an exact solution of equation (4) is not available, an approximate solution will be obtained by the method of harmonic balance. This method is used to seek a periodic solution. In the frequency domain the differential operator $d/d\tau$ is replaced by iw and. consequently, the system of nonlinear differential equations is converted to a set of nonlinear algebraic equations. When this set has a solution with real positive values of frequency and amplitude and real values of the phase angles, it indicates the occurrence of limit-cycle oscillations of the specified form. Thus one seeks a solution of the following form:

$$\overline{W}_{mn}(\tau) = A_{mn} \sin(\omega \tau + \Phi_{mn})$$
 (8-a)

$$W_{mn} = A_{mn} [\cos \Phi_{mn} + j \sin \Phi_{mn}] \sin \omega_{\tau} \qquad (8-b)$$

$$\overline{W}_{mn,\tau} = \omega A_{mn} [j \cos \Phi_{mn} - \sin \Phi_{mn}] \sin \omega_{\tau}$$
 (8-c)

$$\overline{W}_{mn,m} = -\omega^2 A_{mn} [\cos \Phi_{mn} +$$

$$\sin \Phi_{mn} \sin \omega_{\tau}$$
 (8-d)

$$\overline{W}_{mn}\overline{W}_{rs}$$
 $W_{pq}=A_{mn}A_{rs}A_{pq}\{[\cos\Phi_{mn}\cos\Phi_{rs}$

$$cos\Phi_{pq}\text{-}sin\Phi_{mn}sin\Phi_{rs}cos\Phi_{pq}\text{-}cos\;\Phi_{mn}$$

$$\sin \Phi_{rs} \sin \Phi_{pq} - \sin \Phi_{mn} \cos \Phi_{rs} \sin \Phi_{pq}$$
}-
 $i[\sin \Phi_{mn} \sin \Phi_{rs} \sin \Phi_{pq} - \cos \Phi_{mn} \cos \Phi_{rs}$

$$sin\Phi_{pq}$$
- $sin\Phi_{mn}cos\Phi_{rs}cos\Phi_{pq}$ - $cos\Phi_{mn}$

$$\sin\Phi_{rs}\cos\Phi_{pq}]\sin^3\omega_r$$
 (8-e)

Where, $\frac{1}{\sin^3 \omega_\tau = \frac{1}{4} (3\sin \omega_\tau + \frac{3}{4} \sin 3\omega_\tau)$ (8-f)

The second term which is of higher harmonic will be dropped out and:

$$\sin^3 \omega_\tau = \frac{3}{4} \sin \omega_\tau \tag{8-g}$$

Substituting \overline{W}_{mn} from equations (8) into the Duffing type equation (4) and equating separately the real and imaginary parts of the equations, the set of 2(ixj) nonlinear algebraic equations in the unknown variables given by (ixj) amplitudes, ((ixj)-1) phase angles, and the flutter frequency (ω_f) is obtained. These equations are solved numerically by the modified Newton-Raphson algorithm.

III. Smart Structure System with Piezoelectric materials

The intelligent system consists of one or more microprocessors that analyze the responses from the sensors and use integrated control theory command the actuators to apply localized strains/displacements to alter system response. A smart structure has the capability to respond to the external environmental changes (such as loads or shape change) as well as to the internal environment changes (such as damage or failure), see Ref. [20], [21], [24], and [25]. It incorporates the smart material actuators that allow the alteration of system characteristics (such as stiffness or damping) as well as of system response (such as strain or shape) in a controlled manner. In fact a smart structure involves four key elements: actuators, sensors, control strategies, and power conditioning electronics Fig. 8. Smart structures are basically classified into two main types which are, see Ref [20]:

- Passive smart structure: it contains a built in sensing device to continuously monitor the current state and serviceability of the structure. These allow us to have a clear view of how far away from failure a particular structure is.

- Active smart structure: it has embedded sensors to monitor and measure the performance of the structure, then it has the ability to compare the measured data with a certain specified values and has the means of control to perform the corrective action through an embedded actuators.

piezoelectric effect The relates mechanical effects to electrical effects. These effects are highly dependent upon their orientation to the poled axis. It is, therefore, essential to maintain a constant axis numbering scheme, see Fig. 2. All materials, regardless of their relative hardness. follow the fundamental law of elasticity. The elastic properties of the piezoelectric material control how well it will work in particular application. The relationship between stress and strain is Hooke's Law which can be expressed as:

 $\sigma = E \ \epsilon \ \text{or} \ \epsilon = S \ \sigma \ \text{ for isotropic}$ materials where S = 1/E (9) $\sigma_i = E_{ij} \ \epsilon_j \ \text{or} \ \epsilon_i = S_{ij} \ \sigma_j \ \text{for anisotropic}$ materials (10) Fortunately, many of the constants in the formulas above are equal to zero for PZT piezoelectric ceramics. The non-zero constants are.

 S_{11} , S_{22} , S_{33} , S_{12} , S_{13} , S_{23} , S_{44} , and S_{66} with $S_{11} = S_{22}$ and $S_{66} = 2 (S_{11} + S_{12})$

IV. Flutter Control Using Smart Structure

The control system consists of distributed sensors and actuators

attached to or integrated with the plate to such a degree that the distinction between control functionality and structure functionality is blurred, see Ref. [12], [23], and [25]. The main important aspect in developing the active structure is the optimum choice of the materials and devices that can induce strains within the structure see Ref. [21], [22], and [26]. One of the materials that can produce forces and the strains in structure is piezoelectric material. When an electric field is applied, the piezoelectric effect can be made to respond to (or cause) mechanical deformation in many different modes, such as thickness expansion. transverse expansion. thickness shear, or face shear. The piezoelectric materials in general are anisotropic and their electrical and mechanical responses differ, depending upon the axis of applied electric field or axis of mechanical stress or strain. The axes of the piezoelectric material are identified by numerals as shown in Fig. 2, where 1 correspond to length, 2 to width, and 3 to thickness. subscripts are used, where the first number always identifies the axis of the applied electric field. While the second number refers to the axis of induced mechanical strain or applied stress. The polarization axis is always the thickness or the 3 axis. Mechanical stress or strain can take place in all three directions. When an electric field is applied to a film of piezoelectric material, the film dimensions change in the direction of all three axes under stress free conditions. The degree to which these dimensions change relative to the applied field depends on the di constant. So, di can be defined as the stress-free ratio of the developed strain to applied field. For example d₃₁ represents strain developed along axis (1) due to field applied along axis (3).

IV.1 Plate with PVF Piezoelectric Film as Distributed Actuator

A piezoelectric film of poly-Vinylidene-Fluoride (PVF2) is used as spatially distributed actuators. The properties of this piezoelectric film were shown in Table 2. The plate with two layers of (PVF2) film bonded perfectly to its upper and lower surface is shown in Fig. 3. The film used is biaxially polarized during its manufacturing, i.e. the field imposed across its faces will result in a proportional strain along the spatial dimension. As a result of the applied control voltage, an internal strain will be induced in both the (PVF2) and the plate. This strain results in a net stress in each layer to produce spatially uniform in-plane tensile forces. These forces are functions of the applied electric field as well as the elasticity and the thickness ratios. The strain induced in the plate due to the applied field on the piezoelectric layer is determined from the compatibility conditions. At the interface the strain in the plate will be same as that for the piezoelectric layer. The strain induced due to applied electric field is calculated and found to

$$\varepsilon_{x}^{(AV)} = \frac{\alpha}{\alpha q_{1} l_{2}} d_{31} \frac{V}{N_{6}}$$
 (13-a)

$$\varepsilon_{x}^{(AV)} = \frac{\alpha}{\alpha + ib} \quad d_{31} \quad \frac{V}{N_{2}}$$

$$\varepsilon_{y}^{(AV)} = \frac{\alpha + ib}{\alpha + ib} \quad d_{32} \quad \frac{h_{12}}{h_{2}}$$
(13-a)
(13-b)

where: ψ is the measure of the relative mechanical ratio of the structure to the actuator and is given by:

$$\psi = \frac{E_1 h_1}{E_2 h_2}$$
 (13-c)

and a is the plate equilibrium parameter.

When an electric field is applied across both piezoelectric layers in the direction of the arrows shown in Fig. 4, the plate will be in extension, and a will equal to 2. If the field is applied across one piezoelectric layer in the direction of the arrow and reversed on the second, the plate will be deformed in bending, and a will equal to 6. Thus it is to be concluded that the piezoelectric layers

will be more effective in exciting surface strain in bending than in extension.

IV.2 Mathematical Modeling of the Composite Plate

In order to establish the fundamental elastic coupling of the piezoelectricplate system, the static models of the actuator coupled to the plate given by (12-a) and (12-b) is used. The strains displacements relations for the plate with the two piezoelectric layers are

$$\begin{array}{ll} \epsilon_{x} = u^{\circ}_{,x} + (1/2)w^{2}_{,x} - zw_{,xx} + \epsilon_{x}^{(AV)} & (14-a) \\ \epsilon_{y} = v^{\circ}_{,y} + (1/2)w^{2}_{,y} - zw_{,yy} + \epsilon_{y}^{(AV)} & (14-b) \\ \epsilon_{xy} = u^{\circ}_{,y} + v^{\circ}_{,x} + w_{,x}w_{,y} - 2w_{,xy} & (14-c) \end{array}$$

$$\varepsilon_{xy} = u^{0}_{,y} + v^{0}_{,x} + w_{,x}w_{,y} - 2w_{,xy}$$
 (14-c)

As in the classical plate theory, the stress resultants and couples are given

$$[N^{(T)}_{x_1} N^{(T)}_{y_1} N^{(T)}_{xy}] =$$

$$\sum_{k=1}^{3} [\sigma^{(k)}_{x_1}, \sigma^{(k)}_{y_1}, \sigma^{(k)}_{xy}] dz$$

$$[M^{(T)}_{x_1} M^{(T)}_{y_2}, M^{(T)}_{xy}] =$$
(15-a)

$$\sum_{k=1}^{3} \int [\sigma^{(k)}_{x}, \, \sigma^{(k)}_{y}, \, \sigma^{(k)}_{xy}] \, z dz$$
 (15-b)

where the stresses for the kth layer are related to its strain through the constitutive relations:

$$\sigma^{(k)}_{x} = \frac{E_{(k)}}{1 - \upsilon_{(k)}^{2}} (\varepsilon_{x} + \upsilon_{(k)} \varepsilon_{y})$$
 (16-a)

$$\sigma^{(k)}_{x} = \frac{E_{(k)}}{1 - \upsilon_{(k)}^{2}} (\varepsilon_{x} + \upsilon_{(k)} \varepsilon_{y})$$

$$\sigma^{(k)}_{y} = \frac{E_{(k)}}{1 - \upsilon_{(k)}^{2}} (\varepsilon_{y} + \upsilon_{(k)} \varepsilon_{x})$$
(16-a)

$$\sigma^{(k)}_{xy} = G_{(k)} \, \varepsilon_{xy} \tag{16-c}$$

In performing the previous integrations, care must be taken to obtain the correct stiffnesses and piezoelectric forcing terms. The piezoelectric layers and the plate will contribute to the extensional, coupling, and bending stiffnesses of the system while only the piezoelectric layer will produce the forces and moments.

Substituting the strains given equation 13 into stress strain relation 15 and the results into equation 14, we get the expression for the resultant stresses

and couples in the plate with the two upper and lower piezoelectric layer represented in terms of displacements beside the stresses due to piezoelectric strain, see Ref. [12]. If Poisson's ratio for the plate material and the piezoelectric layers are assumed to be the same, then the resultant stresses and couples take the form:

$$N_x^{(T)} = Q_1 - \frac{E_1 h_1}{1 - v^2} ((u^o_{,x} + (1/2) w^2_{,x}) + v (v^o_{,y} + v^o_{,x}))$$

$$(1/2) w_{,y}^{2}]+[(\epsilon_{x}^{(AV)}+\upsilon\epsilon_{y}^{(AV)})]$$
 (17-a)

$$N_y^{(T)} = Q_1 - \frac{E_1 h_1}{1 - v^2} \{ [(v^o_{,y} + (1/2)w^2_{,y}) + v(u^o_{,x} + v^o_{,y})] \}$$

$$(1/2)w^{2}_{,x})]+[(\epsilon_{y}^{(AV)}+\upsilon\ \epsilon_{x}^{(AV)})]\}$$
 (17-b)

$$N_{xy}^{(T)} = Q_1 G_1 h_1 \{ u^0_{,y} + v^0_{,x} + w_{,x} w_{,y} \}$$
 (17-c)

$$M_x^{(T)} = -Q_2 \frac{E_1 h_1^3}{12(1-v^2)} \{W_{,xx} + vw_{,yy}\}$$
 (17-d)

$$M_y^{(T)} = -Q_2 \frac{E_1 h_1^3}{12(1-v^2)} \{ w_{,yy} + vw_{,xx} \}$$
 (17-e)

$$M_{xy}^{(1)} = -Q_2^{-1} \frac{G_1 h_1^3}{6} \{w_{,xy}\}$$
 (17-f)

$$Q_1^{"} = (1+2\frac{1}{\psi})$$
 (18-a)

$$Q_2^{-1} = \{1+2\frac{1}{\psi}[3+6\frac{h_2}{h_1}+4\frac{h_2^2}{h_1^2}]\}$$
 (18-b)

Q1" and Q2" are the contribution to the membrane rigidity and the flexural rigidity of the plate, respectively, due to the piezoelectric layers.

To distinguish between the membrane in-plane forces due to deflection of the plate and the in-plane tensile forces due to applied control voltage, it is preferable to write equations (16-a) and (16-b) in the following form:

$$N_x^{(T)} = N_x + N_x^{(AV)}$$
 (19-a)
 $N_y^{(T)} = N_y + N_y^{(AV)}$ (19-b)

$$N_y^{(T)} = N_y + N_y^{(AV)} \tag{19-b}$$

$$N_x^{(AV)} = Q_1 \frac{-E_1}{1-v^2} \frac{h_1}{v^2} \{ \epsilon_x^{(AV)} + v \epsilon_y^{(AV)} \}$$
 (20-a)

$$N_y^{(AV)} = Q_1 \frac{E_1 h_1}{1 - v^2} \{ \epsilon_y^{(AV)} + v \epsilon_x^{(AV)} \}$$
 (20-b)

The obtained resultant stresses and couples are substituted into equation of equilibrium given in Ref. [13] and [27], to get the equations of motion of the plate with the piezoelectric layers. These equations are nondimensionalized using the same nondimensional parameters given before. The only terms which are not included in the previous equations are the voltage induced in-plane forces. These two terms are nondimensionalized as follows:

$$\begin{split} \overline{n_{\xi}}^{(AV)} &= -\frac{12 a^2}{\pi^4 h_1^2} \{1 + \frac{2}{\psi}\} \{\frac{\alpha}{\alpha + \psi}\} \\ \{d_{31} + \nu d_{32}\} \frac{V}{h_2} \\ \overline{n_{\eta}}^{(AV)} &= \frac{12 a^2 f^2}{\pi^4 h_1^2} \{1 + \frac{2}{\psi}\} \{\frac{\alpha}{\alpha + \psi}\} \\ \{d_{31} + \nu d_{32}\} \frac{V}{h_2} \end{split} \tag{21-b}$$

and the w-equation will be:

$$\begin{split} &\frac{1}{\pi^4} \{ \overline{w}_{,\xi\xi\xi\xi} + 2f^2 \overline{w}_{,\xi\xi\eta\eta} + f^4 \overline{w}_{,\eta\eta\eta\eta} \} - n_\xi^{(AV)} \\ &\overline{w}_{,\xi\xi} - n_\eta^{(AV)} \overline{w}_{,\eta\eta} + \lambda_a \overline{w}_{,\xi} + \lambda_d \overline{w}_{,\tau} + \overline{w}_{,\tau\tau} - \\ &\frac{1}{\pi^4} \{ 12 \frac{a}{h} \left[\overline{u}_{,\xi} \overline{w}_{,\xi\xi} + \upsilon f^2 \overline{u}_{,\xi} \overline{w}_{,\eta\eta} + (\\ 1-\upsilon) f^2 \overline{u}_{,\eta} \overline{w}_{,\xi\eta} + f^3 \overline{v}_{,\eta} \overline{w}_{,\eta\eta} + \upsilon f \overline{v}_{,\eta} \overline{w}_{,\xi\xi} + (\\ 1-\upsilon) \overline{fv}_{,\xi} \overline{w}_{,\xi\eta} \right] + 6 \left[\overline{w}^2_{,\xi} \overline{w}_{,\xi\xi} + f^4 \overline{w}^2_{,\eta} \right] \\ &\overline{w}_{,\eta\eta} + f^2 \overline{w}^2_{,\eta} \overline{w}_{,\xi\xi} + f^2 \overline{w}^2_{,\xi} \overline{w}_{,\eta\eta} + f^2 \overline{w}_{,\xi} \\ &\overline{w}_{,\eta} \overline{w}_{,\xi\eta}] \} = 0 \end{split} \tag{21-c}$$

It is worthwhile to mention that the cavity term and the in-plane forces due to applied loads and thermal stresses terms are dropped out for investigation of the effect of the piezoelectric actuators alone. nondimensional equations are solved by the same procedures shown before. of final form the equation The represents the nondimensional deflection as function of both the aerodynamic loading and damping, and

the in-plane applied forces due to piezoelectric layers. Fig. 5 shows the flutter point for the same weight of the plate with and without piezoelectric materials, where the voltage applied is V = 4.3 x 105 volts. It is clear from the figure that for this particular value of the applied control voltage V, the induced in-plane tensile forces affect the plate flutter by shifting its critical value to about twice the value for the plate without treatment. By increasing the value of the applied voltage the critical aerodynamic loading is shifted more and more toward higher values. The limiting of this process is the operating condition of the plate. In the field of aircraft and spacecraft, the use of high voltage is not recommended from point of view of safety consideration. To avoid the usage of a high voltage, it is necessary to investigate the factors affecting this high voltage. Piezoelectric layers have two distinct effects. Firstly, it increases the plate membrane and flexural rigidities, and secondly, the applied electric field will produce extra in-plane tensile forces. These forces are given in its nondimensional form by equation 20 and are functions of the controlled applied voltage V and the relative mechanical ratio w. In case when the modulus of elasticity and the thickness of these layers are small relative to that of the base plate (as the case of the PVFD2), the first effect is small and may be neglected. On the other hand, the second effect which depends mainly on the piezoelectric material properties beside its elasticity properties will be small consequently high voltage will required to do the task. The higher the values of the piezoelectric constants d₃₁ and d₃₂, the modulus of elasticity E₂, and the thickness h2, the higher the forces and the lower the required voltage.

IV.3 Plate with PZT Piezoelectric Ceramics as Distributed Actuator.

This previous observation encourages the seeking of some other materials with high piezoelectric constants and elasticity modulus. In fact, it is found that the mechanical and electrical properties of the PZT G-1195, PZT HST-41, or PZT G-1278 piezoelectric materials satisfy these requirements. They have higher values of both piezoelectric constants di and the elasticity modulus. But on the other hand, they have higher densities and also they cannot be produced in the form of sheets like PVF2 film. It is found that using the properties of these materials in the previous formulations will decrease the required voltage dramatically. In other words, increasing the critical aerodynamic loading to the same values obtained by using PVF2 will require very low voltage compared the previous case, which acceptable from practical point of view. Fig. 6, shows the flutter point for the plate with and without piezoelectric material, where the voltage applied in this case is V = 80 volts. Fig. 7 shows a comparison between the plate with PVF2 and plate with PZT piezoelectric materials. It is clear from the figure that the PZT material is more effective.

V. Conclusion

The following conclusive statements can be summarized based on the investigations and results obtained.

- For thin plates, where the deflection is at least of the same order of magnitude as the plate thickness, the nonlinear thin plate theory must be used. The nonlinearity, represented by the plate in-plane (membrane) forces created due to large deflection, is the main source that causes the amplitude of the plate deflection during flutter to be limited (limit cycle oscillation).
- The accuracy of the result depends on the number of terms in the assumed series solution. For plates with high aspect ratio and when the direction of the flow is parallel to the longitudinal

direction, the more terms in that direction, the more accurate the obtained results. It is found that using three terms in both directions gives good agreements with the experimental results.

- In-plane applied tensile load has great stabilizing effect by suppressing flutter. These externally applied in-plane loads can be obtained thermally by assembling a pre-stressed plate or electrically by bonding two layers of piezoelectric materials to both the upper and lower surfaces of the plate. When a voltage is applied to these piezoelectric layers, an induced strain in the plate material takes place and consequently tensile in-plane load is obtained. These tensile loads shift the onset of flutter point to about twice the value of the critical dynamic pressure for the plate alone. The important factors that affect this technique are the electrical and mechanical properties of the piezoelectric material with respect to the plate material and the way the voltage is applied.
- From these previous results, it is concluded that using the piezoelectric material is suitable for the prevention and control of flutter, without adversely affecting the weight and cost.

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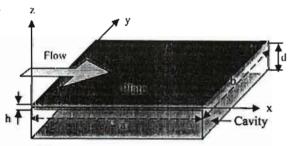


Fig. 1, Geometry of the Plate with Axes System

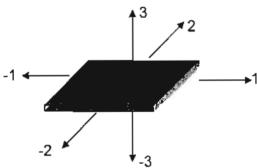


Fig. 2, Numerical Classification of the Axes of the Piezoelectric Film

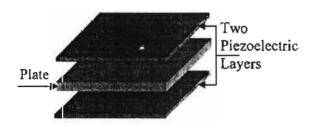
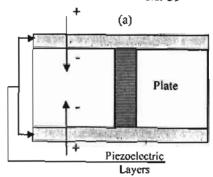


Fig. 3, Plate with Two Piezoelectric Layers at the Top and Bottom



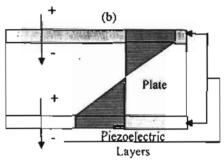


Fig. 4, Plate with Two Piezoelectric Layers Bonded Perfectly to its Upper and Lower Surfaces,

- a) Extension, when the Applied Voltage are in the Same Direction.
- b) Bending, when the Applied Voltage are in Opposite Directions.

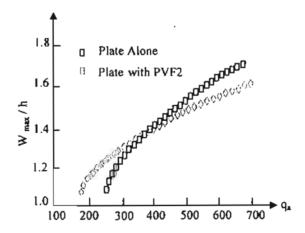


Fig. 5, Flutter Characteristic of the Plate with and without PVF2 Piezoelectric Material (Applied Voltage is 43000 Volts)

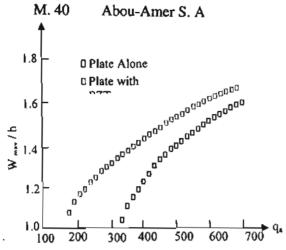


Fig. 6, Flutter Characteristic of the Plate with and without PZT Piezoelectric Material (Applied Voltage is 80 Volts)

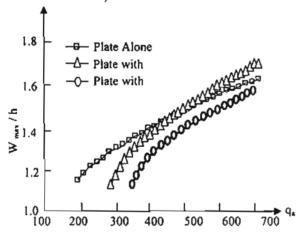


Fig. 7, Comparison between the Plate, the Plate with PVF2, and the Plate with PZT Piezoelectric Materials

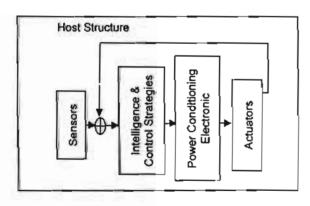


Fig. 8, Smart structure system with it's four basic key elements.

Table 1, Values of α_m and γ_m in the Beam Eigen function or a Clamped Plate.

М	α _m	Ϋ́π
1	4.730040744862704	0.98250221457623
ļ	030	807
2	7.853204624095837	1.00077731190726
	557	905
3	10.99560783800167	0.99996645012540
	100	900
4	14.13716549125746	1.00000144989765
	410	650
3	17.27875965739948	0.99999993734438
	100	300
6	20.42035224562061	1.000000000270759
Ĺ	00	500
ın		
>	(2m+1) π/2	1.0
6		

Table 2, Dimensions and Properties of the Plate and the Treatment Piezoelectric Layers.

	Plate	Piezoelectric -	
Dimensions		Layer	
and Properties		PVDF	PZT
		2	
Availability		Sheet	Segmen
		OZ.	t
		Rolls	
Length (m)	0.7620		38 x 10°
Width (m)	0.1778		15 x 10°
Thickness	0.8128	0.009	0.2500
(x10 ⁻³ m)		to	
		0.800	
Young's	72.398	2.0000	63.000
Modulus (x			
10° N/m²)			
Shear Modulus	27x10 ³		
(x 10 ⁹ N/m ²)			
Poisson's Ratio	0.3300	0.3300	0.3300
Density (x 10 ³	1.6189	1.8000	7.5000
kg/m³)			
Coefficient of	11.700		
Thermal]	
Conductivity			
(μm/m.k)			
Loss Factor	0.0050		
Piezoelectric		d ₃₁	d ₃₁
Strain		=23	=190
Constant (x 10°		$d_{32} = 3$	$d_{32} = 27$
12 V/m)			